

2020/05/02-2020/05/08周报

团队训练

本周无团队训练

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专题

没有专题

比赛

没有比赛

题目

TJOI2019 唱、跳、rap、篮球

分类：生成函数、FFT

一句话题意：有四类人排队，每类人分别喜欢唱、跳、rap、篮球，分别有 a, b, c, d 个人，队伍长度 n 。如果任意 $k, k+1, k+2, k+3$ 四个位置上的人依次喜欢唱、跳、rap、篮球，则不合法，求合法的排列方法数 mod 998244353。 $n, a, b, c, d \leq 1e3$

解法：注意任意两个四人组不可能有交，分别求至少包含 $1, 2, \dots$ 个四人组不合法，求法使用指数型生成函数，最后容斥

```
#include <bits/stdc++.h>
using namespace std;
const int N = 4040;
long long a[N], b[N], nn = 1, rev[N], w1[N], w2[N];
const int mod = 998244353;

inline int power(int di, int ci) {
    int ret = 1;
    while (ci) {
        if (ci & 1)
            ret = (long long)ret * di % mod;
        di = (long long)di * di % mod;
        ci >>= 1;
    }
}
```

```
    }
    return ret;
}
inline long long inv(int x) {
    return power(x,mod-2);
}
inline void NTT(long long *x,int I) {
    int i,j;
    long long t0,t1,*w;
    int k;
    for (i = 0;i < nn; i++)
        if (rev[i] > i)
            swap(x[rev[i]],x[i]);
    w = (I == 1?w1:w2);
    for (i = 1;i < nn; i <= 1) {
        for (j = 0;j < nn; j += (i<<1)) {
            for (k = 0;k < i; k++) {
                t0 = x[j+k],t1 = (long long)w[i*k]*x[i|j+k]%mod;
                x[j+k] = (t0+t1)%mod;
                x[i|j+k] = ((t0-t1)%mod+mod)%mod;
            }
        }
    }
    if (I == -1)
        for (int i = 0;i < nn; i++)
            x[i] = (long long)x[i]*inv(nn)%mod;
}
int half;
int aa,bb,cc,dd,n;
void calc() {
    for (int i = 0;i < half; i++)
        w1[i|half] = power(3,(mod-1)/nn*i);
    for (int i = half-1;i>0; --i)
        w1[i] = w1[i<<1];
    for (int i = 1;i < nn; i++)
        w2[i] = inv(w1[i]);
    NTT(a,1);
    NTT(b,1);
    for (int i = 0;i < nn; i++)
        a[i] = (long long)b[i]*a[i]%mod;
    NTT(a,-1);
    for (int i = n+1;i <= nn; i++)
        a[i] = 0;
}
long long njc[1010];
inline void work(int p) {
    memset(a,0,sizeof(a));
    memset(b,0,sizeof(b));
    for (int i = 0;i <= min(aa-p,n); i++)
        a[i] = njc[i];
}
```

```

    for (int i = 0; i <= min(bb-p,n); i++)
        b[i] = njc[i];
    calc();
    memset(b,0,sizeof(b));
    for (int i = 0; i <= min(cc-p,n); i++)
        b[i] = njc[i];
    calc();
    memset(b,0,sizeof(b));
    for (int i = 0; i <= min(dd-p,n); i++)
        b[i] = njc[i];
    calc();
}

long long C[1010][1010];
long long f[1010];
int main() {
    scanf("%d%d%d%d",&n,&aa,&bb,&cc,&dd);
    C[0][0] = 1;
    for (int i = 0; i <= 1000; i++) {
        C[i][i] = C[i][0] = 1;
        for (int j = 1; j < i; j++)
            C[i][j] = (C[i-1][j]+C[i-1][j-1])%mod;
    }
    njc[0] = 1;
    while (nn <= n+n)
        nn <<= 1;
    half = nn/2;
    for (int i = 1; i < nn; i++)
        rev[i] = (rev[i>>1]>>1)|((i&1)?half:0);
    for (int i = 1; i <= n; i++) {
        njc[i] = njc[i-1]*inv(i)%mod;
    }
    long long ans = 0;
    for (int i = 0; i <= n/4; i++) {
        if (i > aa || i > bb || i > cc || i > dd)
            break;
        work(i);
        f[i] = a[n-4*i]*inv(njc[n-4*i])%mod*C[n-3*i][i]%mod;
        if (i&1)
            ans -= f[i];
        else
            ans += f[i];
    }
    // cout<< i << " " << f[i] << endl;
}
for (int i = n/4; ~i; i--) {
    for (int j = i+1; j <= n/4; j++)
        (f[i] -= f[j]*C[j][i]) %= mod;
}
f[0] += mod;
f[0] %= mod;
ans %= mod;

```

```
ans += mod;  
ans %= mod;  
// cout << ans << endl;  
printf("%lld", f[0]);  
return 0;  
}
```

姜维翰

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题目

cf goodbye 2018 E

题意：一个n点无向图，给出n-1点的度数，问第n个点的所有可能度数，无解输出-1

n=500000

解法：我们可以很容易知道答案的奇偶性，此外若a和b都可行 $a < b$ 则对于 $a < c < b$ 且c和ab奇偶性相同，那么c一定可行

所以只要找出上下界就行

原题中给出了一个定理，利用这个定理以及握手定理可以判定给定的度数是否合法

看上去不能二分，但是这个定理在判出非法的同时你还可以知道是偏大还是偏小，所以可以先二分找一个可靠解，再对上下界二分

```
<code cpp> #include<bits/stdc++.h>
```

```
using namespace std;
```

```
typedef long long ll; typedef double db; typedef complex<double> cp; typedef pair<int,int> pll;
```

```
const int maxn=(int)5e5+9; const int maxm=(int)1e6+9; const ll mod=(ll)998244353; const db  
pi=acos(-1); const db eps=1e-15;
```

```
#define dbg(x) cerr<<#x<<" is "<<x<<endl;
```

```
ll e[maxn]; ll tmp[maxn]; ll sur[maxn]; ll n;
```

```
int ck(ll v){
```

```
int p=0;
int fl=0;
int pos;
for(int i=0;i<=n;i++){
    if(!fl&&(p==n||v<=e[0]||(v>e[p-1]&&v<=e[p]))){
        fl=1;
        tmp[i]=v;
        pos=i;
    }else{
        tmp[i]=e[p];
        p++;
    }
}
sur[n+1]=0;
for(int i=n;i>=0;i--){
    sur[i]=sur[i+1]+tmp[i];
    //printf("$%d\n",sur[i]);
}
for(int i=n-1;i>=0;i--){
    int pp=upper_bound(tmp,tmp+n+1,n-i)-tmp;
    pp=min(pp,i);
    //printf("# %d %lld %d\n",i,sur[i+1],pp);
    if(sur[i+1]>(n-i)*(n-i-1)+sur[0]-sur[pp]+(n-i)*(i-pp+1)){
        if(i<=pos)return 1;
        else return -1;
    }
}
return 0;
```

```
}
```

```
void init(){
```

```
scanf("%d",&n);
for(int i=0;i<n;i++){
    scanf("%lld",&e[i]);
}
sort(e,e+n);
```

```
}
```

```
int main(){
```

```
init();
ll sum=0;
for(int i=0;i<n;i++){
    sum+=e[i];
```

```
}
ll bg,ed;
bg=0;
ed=((ll)n)*(n+1) - sum;
ed=min(ed,n);
ll mid;
while(bg<ed){
    mid=(bg+ed)/2;
    int f=ck(mid);
    //dbg(f);
    //dbg(mid);
    if(f==-1){
        bg=mid+1;
    }else if(f==1){
        ed=mid-1;
    }else{
        break;
    }
}
if(bg==ed&&ck(bg)!=0){
    printf("-1\n");
    return 0;
}
//dbg(mid);
ll m1=mid;
while(bg<m1){
    ll mm=(bg+m1)/2;
    int f=ck(mm);
    if(f){
        bg=mm+1;
    }else{
        m1=mm;
    }
}
ll m2=mid;
while(m2<ed){
    ll mm=(m2+ed+1)/2;
    int f=ck(mm);
    if(f){
        ed=mm-1;
    }else{
        m2=mm;
    }
}
ll eo=sum&1;
for(ll i=bg;i<=ed;i++){
    if(eo==(i&1)){
        printf("%lld ",i);
    }
}
}
```

```
cout<<endl;
```

<code>

本周推荐

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