

# 2020牛客暑期多校训练营（第六场）

## 比赛情况

题号	A	B	C	D	E	F	G	H	I	J	K
状态	-	O	O	-	O	O	∅	O	-	O	O

O 在比赛中通过 ∅ 赛后通过! 尝试了但是失败了- 没有尝试

比赛时间

2020-07-27 12:00-17:00

## 题解

### B - Binary Vector

求  $n$  个  $n$  维  $\{0,1\}$  向量线性无关的概率。

找到分子的通项  $2^{\frac{n(n-1)}{2}} \prod_{i=1}^{n-1} (2^i - 1)$  线性的  $dp$  一下求出来。

```
#pragma GCC optimize(2)
#pragma GCC optimize(3,"Ofast","inline")
#include<bits/stdc++.h>
#define ALL(x) (x).begin(),(x).end()
#define ll long long
#define db double
#define ull unsigned long long
#define pii_pair<int,int>
#define mp_make_pair
#define pb push_back
#define fi first
#define se second
#define rep(i,a,b) for(int i=(a);i<=(b);i++)
#define per(i,a,b) for(int i=(a);i>=(b);i--)
#define show1(a) cout<<#a<<" = "<<a<<endl
#define show2(a,b) cout<<#a<<" = "<<a<<" "; cout<<#b<<" = "<<b<<endl
using namespace std;
const ll INF = 1LL<<60;
const int inf = 1<<30;
const int maxn = 2e7+5;
const int M = 1e9+7;
inline void fastio() {ios::sync_with_stdio(false);cin.tie(0);cout.tie(0);}
ll qpow(ll a,ll b) {ll
s=1;while(b){if(b&1)s=(s*a)%M;a=(a*a)%M;b>>=1;}return s;}

int ans[maxn],inv2[maxn],s[maxn],s2[maxn];
```

```
void init()
{
    int n = 2e7;

    inv2[1] = qpow(2,M-2);
    rep(i,2,n){
        inv2[i] = 1LL*inv2[i-1]*inv2[1]%M;
    }
    rep(i,2,n){
        inv2[i] = 2LL*inv2[i-1]%M*inv2[i]%M*inv2[i]%M;
    }

    ll pow2 = 1;
    s[0] = s2[0] = 1;
    rep(i,1,n) {
        s[i] = 1LL * s[i-1] * pow2 % M;
        pow2 = 2LL * pow2%M;

        s2[i] = 1LL * s2[i-1] * (pow2-1)%M;
    }

    rep(i,1,n){
        ans[i] = 1LL * s[i] * s2[i] % M * inv2[i] % M;
    }
    rep(i,2,n) ans[i] ^= ans[i-1];
}

int main()
{
    fastio();init();
    int _;
    for(cin>>_;;_--){ int n;
        cin>>n;
        cout<<ans[n]<<endl;
    }
    return 0;
}
```

## E - Easy Construction

给一个数字  $k$  要构造一个  $1-n$  的排列，满足对于  $i \in [1,n]$  都存在一个长度为  $i$  子串，使得这个子串内数字的和模  $n$  等于  $k$

首先考虑  $i=n$  的情况，得出结论  $n$  为偶数时  $k = \frac{n}{2}$  才有解，否则  $k=0$  才有解。然后再考虑

如何构造，当  $n$  为偶数时，把  $n$  和  $k$  放最左边，然后依次从右边加入  $i, n-i$ ；当  $n$  为奇数时，先在最左边放  $n$ ，然后依次放入  $i, n-i$ 。

```
#include<bits/stdc++.h>
#define ALL(x) (x).begin(),(x).end()
#define ll long long
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#define ull unsigned long long
#define pii_ pair<int,int>
#define mp_ make_pair
#define pb push_back
#define fi first
#define se second
#define rep(i,a,b) for(int i=(a);i<=(b);i++)
#define per(i,a,b) for(int i=(a);i>=(b);i--)
#define show1(a) cout<<#a<<" = "<<a<<endl
#define show2(a,b) cout<<#a<<" = "<<a<<"; "<<#b<<" = "<<b<<endl
using namespace std;
const ll INF = 1LL<<60;
const int inf = 1<<30;
const int maxn = 5e5+5;
inline void fastio() {ios::sync_with_stdio(false);cin.tie(0);cout.tie(0);}

int main()
{
    fastio();
    int n,k;
    cin>>n>>k;
    if(n%2==0){
        if(k!=n/2) cout<<-1<<endl;
        else{
            cout<<n<<" "<<k<<" ";
            rep(i,1,k-1) cout<<i<<" "<<n-i<<" ";
            cout<<endl;
        }
    }else{
        if(k) cout<<-1<<endl;
        else{
            cout<<n;
            rep(i,1,n/2) cout<<" "<<i<<" "<<n-i;
            cout<<endl;
        }
    }
    return 0;
}
```

## J - Josephus Transform

对排列  $1,2,3,\dots,n$  做  $m$  次操作。每次操作是进行  $x$  次  $k$  约瑟夫问题。求最后的排列。

把操作看成置换，如果已知一次  $k$  约瑟夫问题的置换，那么可以用类似快速幂的方法在  $n \log x$  得到答案。考虑如何求一次  $k$  约瑟夫问题的置换，用线段树暴力模拟就行，复杂度为  $n \log n$  所以总复杂度  $nm(\log n + \log x)$

```
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#define ALL(x) (x).begin(),(x).end()
#define ll long long
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#define rep(i,a,b) for(int i=(a);i<=(b);i++)
#define per(i,a,b) for(int i=(a);i>=(b);i--)
#define show1(a) cout<<#a<<" = "<<a<<endl
#define show2(a,b) cout<<#a<<" = "<<a<<"; "<<#b<<" = "<<b<<endl
using namespace std;
const ll INF = 1LL<<60;
const int inf = 1<<30;
const int maxn = 1e5+5;
inline void fastio() {ios::sync_with_stdio(false);cin.tie(0);cout.tie(0);}

int a[maxn],n,b[maxn],tmp[maxn];
int tr[maxn<<2];
void build(int id,int l,int r)
{
    tr[id] = 0;
    if(l==r) {tr[id]=1;return ;}
    int mid = (l+r)>>1;
    build(id<<1,l,mid);build(id<<1|1,mid+1,r);
    tr[id] = tr[id<<1] + tr[id<<1|1];
}
void update(int id,int stl,int str,int pos)
{
    if(stl==str){
        tr[id] = 0;
        return ;
    }
    int mid = (stl+str)>>1;
    if(pos<=mid) update(id<<1,stl,mid,pos);
    else update(id<<1|1,mid+1,str,pos);
    tr[id] = tr[id<<1] + tr[id<<1|1];
}
```

```

int query(int id,int stl,int str,int l,int r)
{
    if(stl==l && str==r){
        return tr[id];
    }
    int mid = (stl+str)>>1;
    if(r<=mid) return query(id<<1,stl,mid,l,r);
    else if(l>mid) return query(id<<1|1,mid+1,str,l,r);
    else return query(id<<1,stl,mid,l,mid) +
query(id<<1|1,mid+1,str,mid+1,r);
}
int query2(int id,int l,int r,int k)
{
    if(l==r) return l;
    int mid = (l+r)>>1;
    if(tr[id<<1]>=k) return query2(id<<1,l,mid,k);
    else return query2(id<<1|1,mid+1,r,k-tr[id<<1]);
}
void perm(int *a,int *b,int x)
{
    while(x){
        if(x&1){
            rep(i,1,n) tmp[i] = a[b[i]];
            rep(i,1,n) a[i] = tmp[i];
        }
        rep(i,1,n) tmp[i] = b[b[i]];
        rep(i,1,n) b[i] = tmp[i];
        x>>=1;
    }
}
int main()
{
    fastio(); int m,k,x;
    cin>>n>>m;
    rep(i,1,n) a[i] = i;
    while(m--){
        cin>>k>>x;
        build(1,1,n);
        int last = 0;
        rep(i,1,n){
            int r = last==n?0:query(1,1,n,last+1,n);
            if(r>=k){
                int pre = last?query(1,1,n,1,last):0;
                b[i] = query2(1,1,n,k+pre);
                update(1,1,n,b[i]);
                last = b[i];
            }else{
                int tt = k - r;
                tt %= (n-i+1);
                if(tt == 0) tt = n-i+1;
                b[i] = query2(1,1,n,tt);
            }
        }
    }
}

```

```
        update(1,1,n,b[i]);  
        last = b[i];  
    }  
}  
perm(a,b,x);  
}  
rep(i,1,n) cout<<a[i]<<" \n"[i==n];  
return 0;  
}
```

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